

Projectile launched at an angle Practice Problem

Example 1: (from powerpoint)

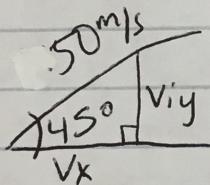
A projectile is launched at 50 m/s at an angle of 45° from the horizontal. It lands at a place level with the place it was launched from.

- (a) Find time of flight ($t_{\text{total}} = ?$)
- (b) Find maximum height of projectile ($d_y = ?$)
- (c) Find horizontal range ($d_x = ?$)

- ① Find V_x and V_{iy} components

using $V_x = V_i \cos \theta$

$$V_{iy} = V_i \sin \theta$$



$$V_x = 50\text{ m/s} \cos 45^\circ = 35.4\text{ m/s}$$

$$V_{iy} = 50\text{ m/s} \sin 45^\circ = 35.4\text{ m/s}$$

- * once you find your V_x & V_{iy} using formulas from above, you no longer need to use the $45^\circ + 50\text{ m/s}$.

Givens:

horizontal
 $V_x = 35.4\text{ m/s}$

vertical
 $V_{iy} = 35.4\text{ m/s}$

- (a) Find time: $V_f = V_{iy} + gt$
 $0\text{ m/s} = 35.4\text{ m/s} + (-9.8\text{ m/s}^2)t$

$$\begin{array}{rcl} -35.4 & -35.4 \\ \hline -35.4 & = -9.8 & t \\ \hline -9.8 & & \end{array}$$

$$3.6\text{ s} = t \rightarrow \text{this is the time for } \frac{1}{2} \text{ of its flight}$$

to find total time, multiply $\frac{1}{2}$ time by 2.

$$3.6\text{s} \times 2 = \boxed{7.2\text{s}}$$

⑥ Find $dy = ?$

use $\frac{1}{2}$ time

$$dy = v_{iy} t + \frac{1}{2} g t^2$$
$$dy = (35.4\text{m/s})(3.6\text{s}) + \frac{1}{2} (-9.8\text{m/s}^2)(3.6\text{s})^2$$
$$\boxed{dy = 63.9\text{m}}$$

⑦ Find $dx = ?$

$$v_x = \frac{dx}{t} \rightarrow dx = v_x(t)$$

use full time

$$dx = (35.4\text{m/s})(7.2\text{s})$$
$$\boxed{dx = 254.88\text{m}}$$